

$$6.1) M_{\text{Pl}}^2 = \frac{M_{\text{Pl}}^2}{(M_{\text{Pl}} R)^n}, \quad M_{\text{Pl}} \sim 10^{16} \text{ TeV}$$

IF $M_{\text{Pl}} \sim 13 \text{ TeV}$, then the LHC could be able to detect gravitons escaping into extra dimensions

$$R^n = M_{\text{Pl}}^2 (M_{\text{Pl}})^{-(n+2)}$$

$$R = \frac{1}{M_{\text{Pl}}} \left(\frac{M_{\text{Pl}}}{M_{\text{Pl}}} \right)^{2/n}$$

$$\sim \frac{1}{13 \text{ TeV}} \left(\frac{10^{16}}{13} \right)^{2/n}$$

$$= 0.0769 (\text{TeV})^{-1} \cdot (7.69 \times 10^{14})^{2/n}$$

$$R = 0.0769 \cdot (5.91 \times 10^{29})^{1/n} \text{ TeV}^{-1}$$

$$\text{Converting } 1 \text{ TeV}^{-1} = 2 \cdot 10^{-17} \text{ cm}$$

$$R = (1.59 \cdot 10^{-17}) (5.91 \times 10^{29})^{1/n} \text{ cm}$$

$$\boxed{n=1: R \sim 10^{13} \text{ cm}}$$

*The existence of this large dimension would have noticeable effects on Newtonian gravity at the solar system scale which have not been detected.

$$\boxed{n=2: R \sim 0.0117 \text{ cm} = 117 \mu\text{m}}$$

*The size of these dimensions already pushes at the limit of our most sensitive tests of gravity on small scales.