

$$4.1) J(x) = \delta^{(2)}(\vec{x} - \vec{x}_1) + \delta^{(2)}(\vec{x} - \vec{x}_2)$$

$$W(J) = -\frac{1}{2} \int \frac{d^3k}{(2\pi)^3} J^*(k) \frac{1}{k^2 - m^2 + i\epsilon} J(k)$$

$$J(k) = \int d^3x e^{-ikx} J(x) = \int dx^0 e^{-ik^0 x^0} (e^{-i\vec{k} \cdot \vec{x}_1} + e^{-i\vec{k} \cdot \vec{x}_2}) = J_1(k) + J_2(k)$$

$$W(J) = -\int \frac{d^3k}{(2\pi)^3} J_2^*(k) \frac{1}{k^2 - m^2 + i\epsilon} J_1(k)$$

$$= -\int dx^0 \int dy^0 \int \frac{d^3k}{(2\pi)^3} \frac{1}{k^2 - m^2 + i\epsilon} e^{-ik^0(x-y)^0} e^{-i\vec{k} \cdot (\vec{x}_1 - \vec{x}_2)}$$

$$= -\int dx^0 \int dy^0 \int \frac{dk^0}{2\pi} e^{-ik^0(x-y)^0} \int \frac{d^2k}{(2\pi)^2} \frac{1}{k^2 - m^2 + i\epsilon} e^{-i\vec{k} \cdot (\vec{x}_1 - \vec{x}_2)}$$

$$W(J) = \int dx^0 \int \frac{d^2k}{(2\pi)^2} \frac{1}{k^2 + m^2} e^{-i\vec{k} \cdot (\vec{x}_1 - \vec{x}_2)}$$

$$Z[J] = Z[J=0] e^{W(J)}$$

$$= \langle 0 | e^{-iHT} | 0 \rangle = e^{-iET}$$

$$E = -\int \frac{d^2k}{(2\pi)^2} \frac{1}{k^2 + m^2} e^{-i\vec{k} \cdot (\vec{x}_1 - \vec{x}_2)}$$

$$= -\frac{1}{(2\pi)^2} \int_0^\infty dk k \int_0^{2\pi} d\vartheta \frac{1}{k^2 + m^2} e^{-ik|\vec{x}_1 - \vec{x}_2| \cos\vartheta}$$

$$= -\frac{1}{2\pi} \int_0^\infty dk \frac{k}{k^2 + m^2} J_0(k|\vec{x}_1 - \vec{x}_2|)$$

$$E = -\frac{1}{2\pi} J_0(m|\vec{x}_1 - \vec{x}_2|)$$

$$x = |\vec{x}_1 - \vec{x}_2|$$

$$E = -\frac{1}{2\pi} J_0(mx)$$

$$\vec{F} = -\vec{\nabla} E$$

$$\vec{F} = -\frac{m}{2\pi} J_1(mx) \hat{x}$$

$$J(x) = \delta^{(D)}(\vec{x} - \vec{x}_1) + \delta^{(D)}(\vec{x} - \vec{x}_2)$$

$$W(J) = -\frac{1}{2} \int \frac{d^{D+1}k}{(2\pi)^{D+1}} J^*(k) \frac{1}{k^2 - m^2 + i\epsilon} J(k)$$

$$W(J) = \int dx^0 \int \frac{d^Dk}{(2\pi)^D} \frac{1}{k^2 + m^2} e^{-i\vec{k} \cdot \vec{x}}$$

$$E = -\int \frac{d^Dk}{(2\pi)^D} \frac{1}{k^2 + m^2} e^{-i\vec{k} \cdot \vec{x}}$$

$$= -\int_0^\infty \frac{dk}{2\pi} \frac{k^{D-1}}{k^2 + m^2} \int \frac{d\Omega_{D-1}}{(2\pi)^{D-1}} e^{-i\vec{k} \cdot \vec{x}}$$

$$= -\int_0^\infty \frac{dk}{2\pi} \frac{k^{D-1}}{k^2 + m^2} \frac{1}{(2\pi)^{D-1}} \int_{\varphi_1=0}^{\pi} d\varphi_1 \int_{\varphi_2=0}^{\pi} d\varphi_2 \dots \int_{\varphi_{D-1}=0}^{2\pi} d\varphi_{D-1} \sin^{\varphi_1-2}(\varphi_1) \sin^{\varphi_2-3}(\varphi_2) \dots \sin(\varphi_{D-2}) e^{-i\vec{k} \cdot \vec{x}}$$

$$E = -\frac{1}{(2\pi)^{D-1}} \int_0^\infty dk \frac{k^{D-1}}{k^2 + m^2} \left(\prod_{j=1}^{D-2} \int_0^{\pi} d\varphi_j \sin^{\varphi_j-1}(\varphi_j) \right) e^{-ikx \cos\vartheta}$$